

WORK ENERGY

NJ-OER TOPIC-7

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Open Textbook Collaborative

The <u>Open Textbook Collaborative</u>. (OTC) project is a statewide project managed by Middlesex College along with assistance from Brookdale Community College, Ocean County College, Passaic County Community College, and Rowan University.

The project engages a consortium of New Jersey community colleges and Rowan University to develop open educational resources (OER) in career and technical education STEM courses.

The courses align to <u>career pathways in New Jersey's growth industries</u> including health services, technology, energy, and global manufacturing and supply chain management as identified by the New Jersey Council of Community Colleges.

General Physics I

Moe Tabanli

Learning Outcomes

recognize the definition of work, kinetic energy and potential energy

identify the mathematical quantities which effect the energy and be able to calculate energy of a system

distinguish between conservative and non-conservative forces and their effect to transformation of energy

determine the total energy change of a system and to state what energy conservation means

Concepts

• F = Force

- d = Displacement
- θ = Angle between the force and the displacement vector
- W = Work
- K=spring coefficient
- Wnc= Work done by non-conservative forces
- KE = Kinetic Energy
- PE = Potential Energy
- Ei = Initial total energy
- Ef = Final total energy

Units

SI Units Force is in Newton's "N" Energy and workdone is in Joules "J" Mass is in kilogram "kg" Angle is in degrees or radian

Energy and work done are scalar quantities

Formulas

Definitions $W = F.d = F d cos(\theta)$ $KE = \frac{1}{2} mv^2$ $PEs=\frac{1}{2}k\Delta x^2$ or $PEs=\frac{1}{2}k\Delta y^2$ or $PEs=\frac{1}{2}kd^2$ PEg=mgh E=KE+PE=KE+PEg+PEs $E=\frac{1}{2}mv^2+mgh+\frac{1}{2}kd^2$

Process Equations If there is no external non conservative forces, then Ef=Ei Ef-Ei=O or KEi+PEi=KEf+PEf If there are external non conservative forces, then Ef-Ei=WNC or WNC+KEi+PEi=KEf+PEf

KEY STRATEGIES FOR WORK DONE PROBLEMS

Draw a free body diagram, identify forces and the angles Each force has its own magnitude and angle with respect to the motion General formula W = F d cos(theta) is always valid for constant force Perpendicular forces does zero work (theta=90 degrees) Parallel forces does positive work (theta=0 degrees) Opposite forces does negative work (theta=180 degrees) Diagonal forces does work based on their parallel components W = F(parallel) d

On a diagonal path, forces does work based on the parallel component of displacement

W= F d(parallel)

Work Done Model Problem

Q: 1a) How much work is done on the lawn mower by the person in the figure if he exerts a constant force of 75.0N at an angle 60^o below the horizontal and pushes the mower 24.0 meters? 1b) How much work is done by the normal force and gravity 1c) There is also friction with magnitude of 20N. What is the work done by the friction.



Hint: Each force has its own magnitude and angle

Work done by external force friction

Use 60 degrees as the angle

Work done by gravity and the normal force Work done by the

For this motion, Normal force and the force of gravity are perpendicular which makes theta=90 degrees. cos(90)=0 Friction is the opposing force for this motion. Which makes theta=180 degrees and workdone negative

CLASSWORK ON WORK DONE

Q) 4.8 Newton's force is applied to move and object 2.5 meters. Find the work done for each of the cases below. First obtain the angle between the force and the displacement by graphing the motion and force.

Force Direction	Displacement Direction	The Angle	Work Done
North	East		
45 degrees Northwest	North		
-i direction (-x direction)	i direction (+x direction)		
20 degrees North of East	40 degrees South of East		

Graphical Interpretation of Work



In a Force vs distance graph, the area under the curve is the work done.

If the area is above the x-axis it counts as positive work

If the area is below the x-axis it counts as negative work

If Force is a piecewise defined function and it is segmented, work done should be calculated for each segment. The sum of the areas gives the net work done

Graphical Interpretation of Work Model Problem

Q2) A variable Force is acting on an object for 5.00 meters. The maximum force is 2.00 Newtons. Force vs distance graph is provided. Find the work done for each segment and find the net work done on the object.



WORK ENERY THEOREM

- KE = $\frac{1}{2}$ m v²
- KEf-KEi = W
- $\frac{1}{2}$ mvf² $\frac{1}{2}$ m vi² = Fd cos(theta)

MODEL PROBLEM

Q) A girl with 42kg mass is rode an 8 kg bicycle for 5.0 meters. Her initial speed is 6.0 m/s

A) What is the work done if her final speed is 8.0 m/s?

B) What is the work done if her final speed is 4.0 m/s?

C) Find the average force for each case. Identity the dominant force as force of friction or force of pedaling.

GRAVITATIONAL POTENTIAL ENERGY

B A

Work done for conservative forces can be expressed as potential energy.
Conservative forces are path independent.
The change in gravitational potential energy (ΔPEg) between points A and B is independent of the path.

 $\Delta PEg = mg \Delta h$ for any path between the two points. PEi= m g hi PEf=m g hf

Elastic Potential Energy



 Work is done to deform the guitar string, giving it potential energy. When released, the potential energy is converted to kinetic energy and back to potential as the string oscillates back and forth. A very small fraction is dissipated as sound energy, slowly removing energy from the string.

Elastic Potential Energy



Force starts from zero and goes to Fmax=kx, k is the spring constant So Favg=½ kx and displacement is x. Angle is zero degrees PEs=½ k x² for horizontal springs PEs=½ k y² for vertical springs PEs=½ k d² for diagonal springs

WORK ENERGY THEOREM CONSERVATION OF ENERGY

- W = **F.d** = F d cos(θ)
- $KE = \frac{1}{2} mv^2$
- PEs=½ kd²
- PEg=mgh
- E=KE+PE=KE+ PEg+PEs
- E=½ mv²+mgh+½ kd²
- Ef=Ei energy is conserved
- or Ef-Ei=WNC work is done by nonconservative forces

PROCESS EQUATIONS

- When a system goes from an initial state to a final state, initial conditions determines the final state.
- Depending on the problem there are two cases
- If there are no external forces, nor friction and work done by nonconservative forces is zero then
- Ef-Ei=0 or Ef=Ei
- KEi+PEi=KEf+PEf
- If there are external forces, such as friction or an external push/pull then work done by nonconservative forces is not zero
- Ef-Ei=WNC
- WNC+KEi+PEi=KEf+PEf

KEY STRATEGIES

- Draw the system, identify initial and final states
- Using numerical values and variable given in the problem calculate the initial energy
- Using numerical values and variables given in the problem calculate or write an expression for the final energy
- Using Ef=Ei or Ef-Ei=WNC find the unknown

KEY WORDS THAT IMPLIES NUMBERS

At rest: vi=0 , zero kinetic energy

Stops: vf=0, zero kinetic energy

Hits the ground: hf=0, zero gravitational potential energy

Unstretched spring: zero elastic potential energy

No friction nor external forces: WNC=0, energy is conserved

MODEL PROBLEM-ENERGY CONSERVATION



- The speed of a roller coaster increases as gravity pulls it downhill and is greatest at its lowest point. Viewed in terms of energy, the roller-coaster-Earth system's gravitational potential energy is converted to kinetic energy. If work done by friction is negligible, all ΔPE_g is converted to KE.
- QUESTION: Determine the speed of the roller coaster as it goes down 25.0 meters

ACTIVITY ENERGY CONSERVATION



- Open Phet Skatepark simulation <u>https://phet.colorado.edu/sims/html/energy-skate-park_en.html</u>
- Click on grid, click on speed, energy and make sure friction is zero
- Release the skater at various heights. Estimate the speed at the bottom of the ramp using conservation of energy and compare it with the simulation

ACTIVITY



For each problem below calculate the final velocity numerically and compare it with the simulation.

Q1: A 60kg skater goes down on a frictionless ramp with 4 meters height. Find the velocity at the end of the ramp Q2: A 50kg skater goes down on a frictionless ramp with 3.5 meters height. Find the velocity at the end of the ramp Q3: A 60kg skater goes down on a frictionless ramp with 2.5 meters height. Find the velocity at the end of the ramp. Q4: Change the track and verify that the final speed is path independent. Change gravity and show that vf depends on g

Q4: Come up with your own problem. Solve it numerically and compare it with the simulation.

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MODEL PROBLEM: ENERGY CONSERVATION FOR ELASTIC POTENTIAL



- A toy car is pushed by a compressed spring and coasts up a slope after it is released. Assuming
 negligible friction, the potential energy in the spring is first completely converted to kinetic
 energy, and then to a combination of kinetic and gravitational potential energy as the car rises.
 The details of the path are unimportant because all forces are conservative
- Q) If a 0.25 kg toy car is compressed by 0.4 meters by a spring with a spring constant k=20N/m and released. What would be its speed at the elevation of 0.16 meters.

NON CONSERVATIVE FORCES-FRICTION



- The amount of the happy face erased depends on the path taken by the eraser between points A and B, as does the work done against friction. Less work is done and less of the face is erased for the path in (a) than for the path in (b). The force here is friction, and most of the work goes into thermal energy that subsequently leaves the system.
- Energy is lost WNC is NEGATIVE

NON-CONSERVATIVE EXTERNAL FORCES



 A person pushes a crate up a ramp, doing work on the crate. Friction and gravitational force (not shown) also do work on the crate; both forces oppose the person's push. As the crate is pushed up the ramp, it gains mechanical energy, implying that the work done by the person is greater than the work done by friction.

ACTIVITY WNC DUE TO FRICTION



- Open Phet Skatepark simulation <u>https://phet.colorado.edu/sims/html/energy-skate-park/latest/energy-skate-park_en.html</u>
- Click on grid, click on speed, energy and make sure friction is NOT ZERO
- Release the skater at various heights. Measure the speed using the speedometer
- Find the work done by non-conservative forces
- For enhancement activity try to calculate the average friction force and the coefficient of friction. The parabolic track can be approximated as a diagonal path with 53 degrees slope. Use W=-f d and f=mu N

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ACTIVITY WNC DUE TO FRICTION



For each problem measure the final velocity and calculate the work done by friction. Try to estimate the average force afterwards.

Q1: A 60kg skater goes down on a ramp with friction from 4 meters height. Measure its final velocity and calculate WNC

Q2: A 50kg skater goes down on a ramp with lots of friction from 3.5 meters height. Measure its final velocity and calculate WNC

Q4: Change the track, verify that the final speed DEPENDS on the path. Obtain the final speed for each track, find WNC

Q4: Build your own track using the playground option with some friction. Investigate the path dependence of vf.

POWER

Power is the rate of applied or dissipated energy

P= E/t

P=W/t

Power has SI unis of J/s or Watts

If an object moves with constant speed against friction, there should be an external applied force

P = F v

MODEL PROBLEM

Q: A conveyer belt moves a box horizontally with 0.40 m/s speed using a machine with 10 Watts output.

A) Find the average applied force.

B) Find the force of friction

C) Find the energy consumption if the machine is operated for one minute. Verify that this energy matches with the work done by the force for moving an object with 0.40 m/s speed for 60 seconds. Find "d" first.

REFERENCES

- Slide 1: Image by Myriams-Fotos from Pixabay
- Slides 7,9,13-15,20,23-25: Open Stax Textbook
- Slides 21-22, 26-27: Screenshot from PhET Interactive Simulations University of Colorado Boulder <u>https://phet.colorado.edu</u>